

Planet/Binary Degeneracy I

- High-magnification events with double-peak structure
- Not only planets but also very wide or very close binaries can also produce such a perturbations.
- Can we distinguish them without detailed modelling?

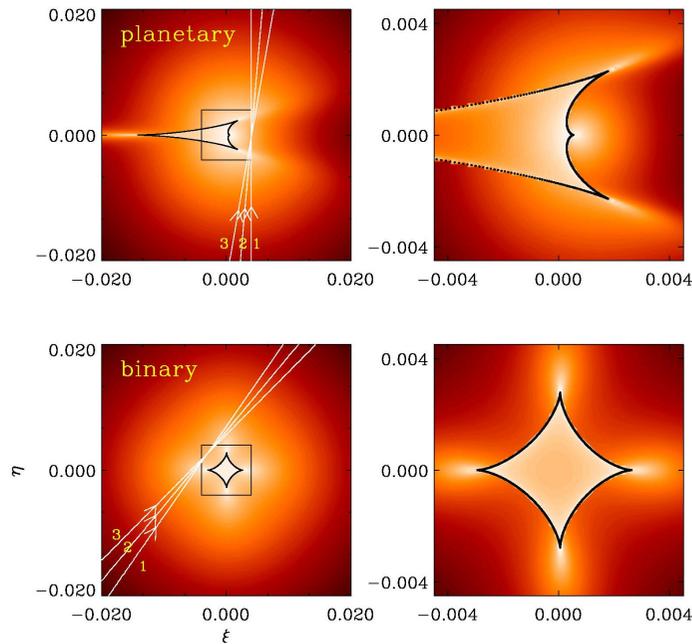


Fig 1. Magnification pattern maps in the central perturbation region of a planetary (upper panels) and binary lensing events, respectively. Right panels are blow-ups of the left panels.

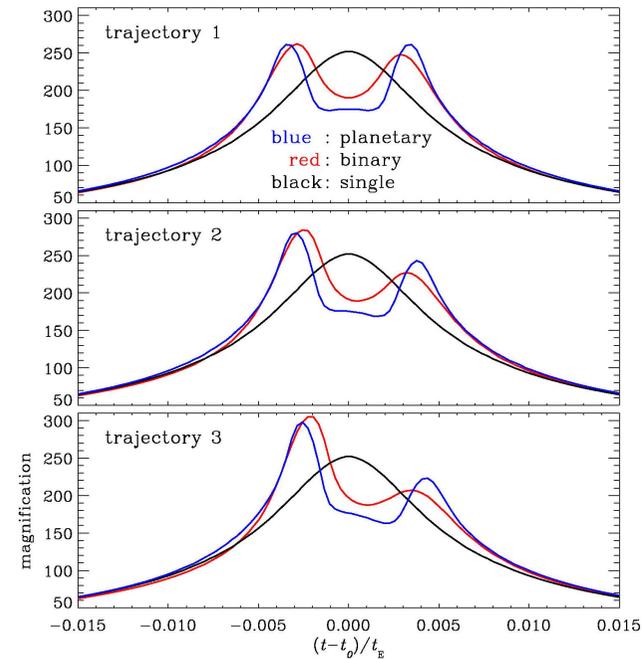
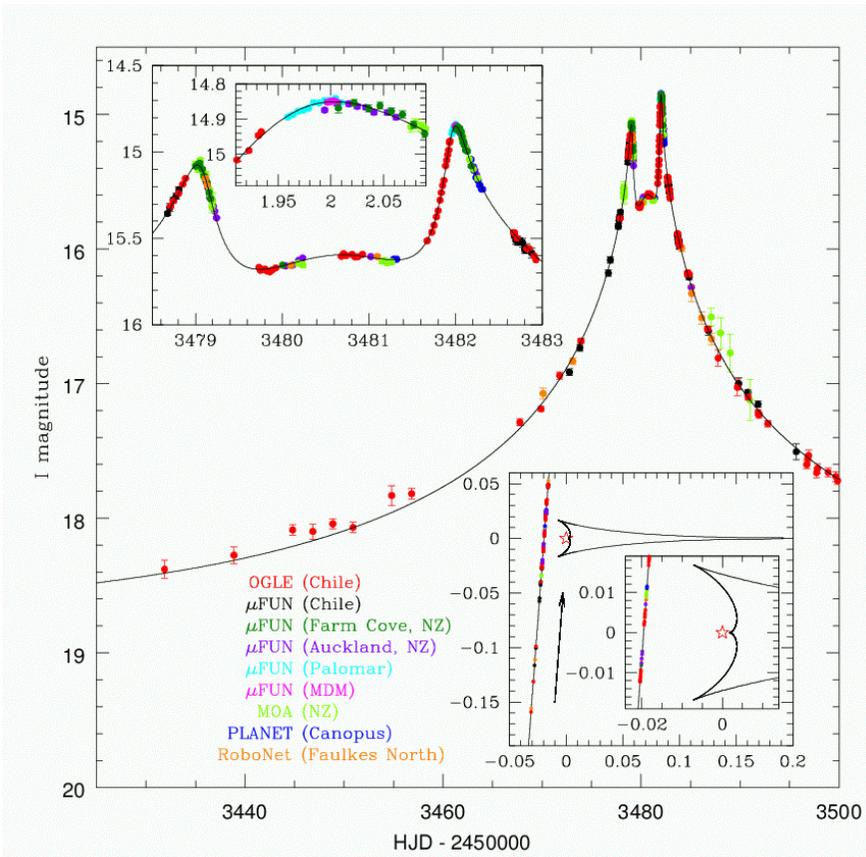


Fig 2. Light curves resulting from the source trajectories in the maps of Fig. 1.

□ An example of a high-magnification events with double-peak structure



- MACHO 99-BLG-47
- OGLE-2005-BLG-071
- OGLE-2007-BLG-349/MOA-2007-BLG-379
- OGLE-2007-BLG-514
- OGLE-2007-BLG-137/MOA-2007-BLG-091

Fig 3. Light curve of the microlensing event OGLE-2005-BLG-071. It shows a double-peak structure near the peak.

□ Difference in the morphology

- A simple diagnostic that can be used to immediately distinguish between the perturbations caused by the planetary and binary companions.
- The diagnostic is based on the difference in the shape of the intra-peak region of the light curve.
 - ▷ **Binary lensing**: The shape is smooth and concave.
 - ▷ **Planetary lensing**: either boxy or convex
- The convex structure for planetary lensing is due to the small, weak cusp between the two strong cusps.
- Good coverage of the intra-peak region is very important.
- See the light curve of OGLE-2005-BLG-071 again.

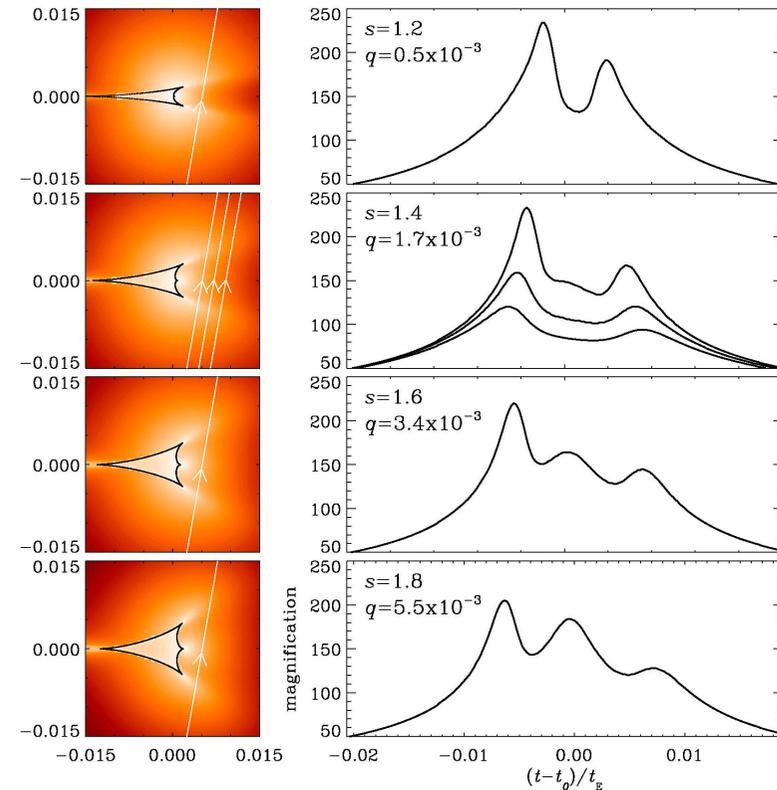


Fig 4. Variation of the planetary light curves with double peaks.

Planetary Feature under Severe Finite-Source Effect

- High-magnification events with severe finite-source effect
- Effect of finite-source effect on perturbation pattern
 - As the angular extent of the source size becomes bigger, the effect becomes more important. As the effect increases, the planetary signal is attenuated.
 - It is believed that the signal is completely washed out when the source size is substantially greater than the caustic size. → *Is this true?*
 - We find that perturbations with fractional magnification excess $\geq 5\%$ survive when the source star is roughly 4 times bigger than the caustic.

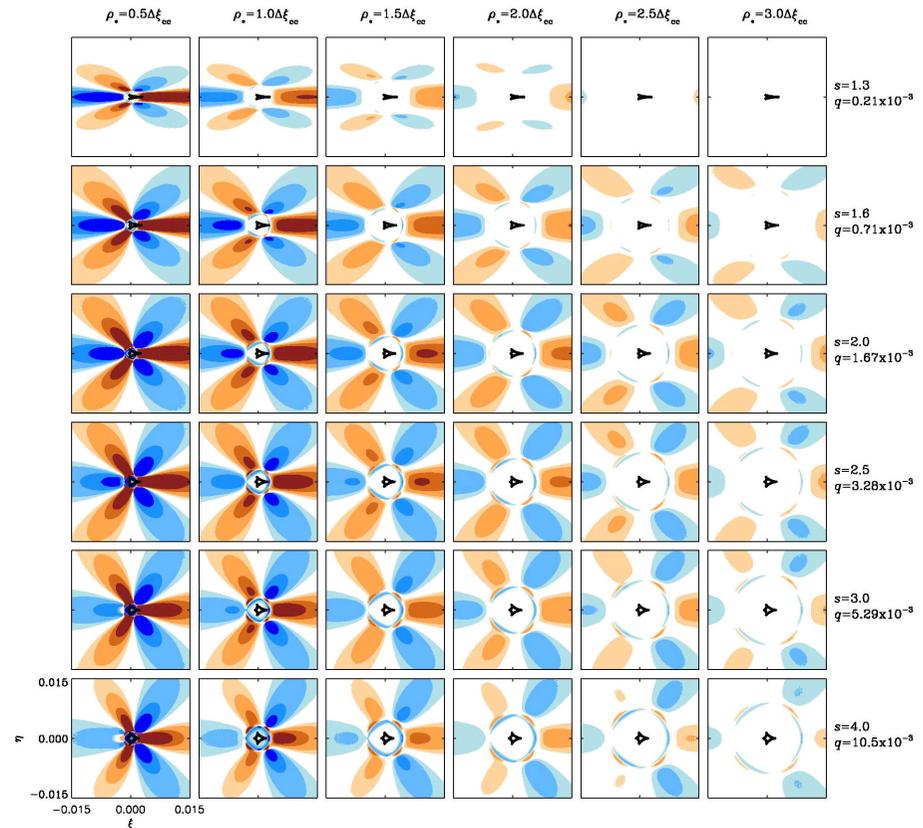


Fig 5. Variation of perturbation pattern depending on finite-source effect.

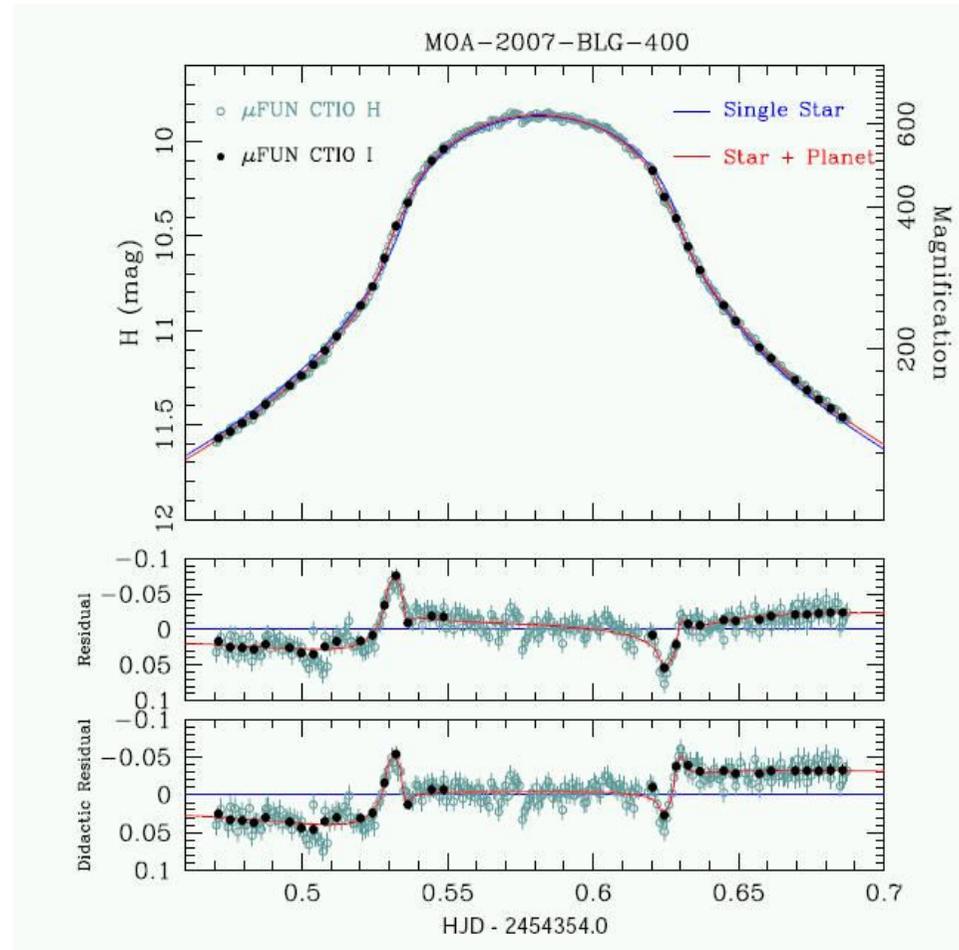


Fig 6. Light curve of the microlensing event MOA-2007-BLG-400

□ **Characteristic Features:** characteristic features that commonly appear in the perturbation patterns of planetary lens systems affected by severe finite-source effect

- **Localized, arc-shaped perturbation** regions around the circle with radius corresponding to the radius of the source star.
- These features form in and around a circle with its center located at the caustic center and a radius corresponding to that of the source star.
- The light curve of an event where the source crosses these features will exhibit a distinctive signal that is characterized by short-duration perturbations of either positive or negative excess and a flat residual region between these short-duration perturbations.

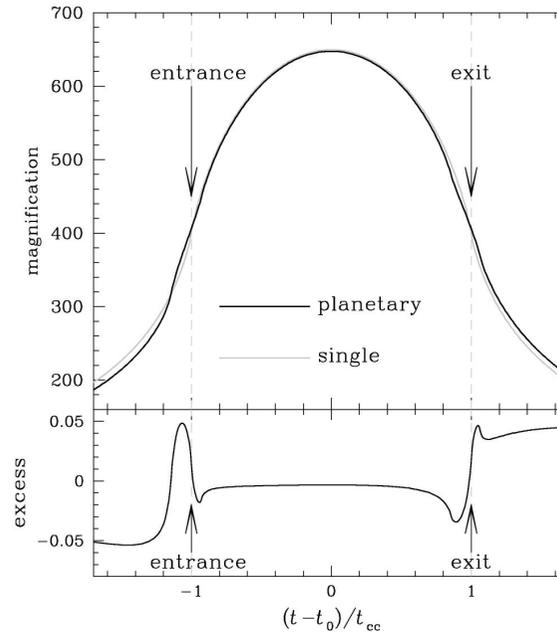


Fig 8. Light curve and residual of an example planetary lensing event under severe finite-source effect.

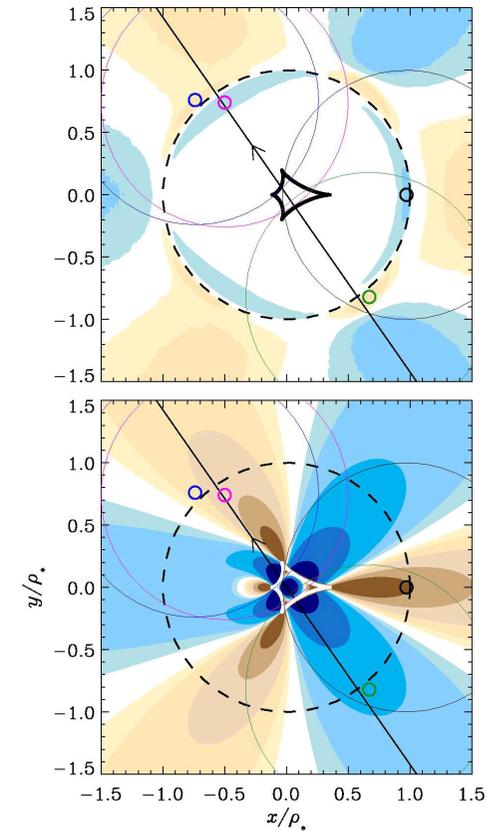


Fig 7. Morphology of central perturbation of a planetary lens system.

Planet/Binary Degeneracy II

- Signals of events under severe finite-finite can also be produced by a binary companion.
How can we distinguish the planetary and binary interpretations?

- Comparison of the perturbation patterns

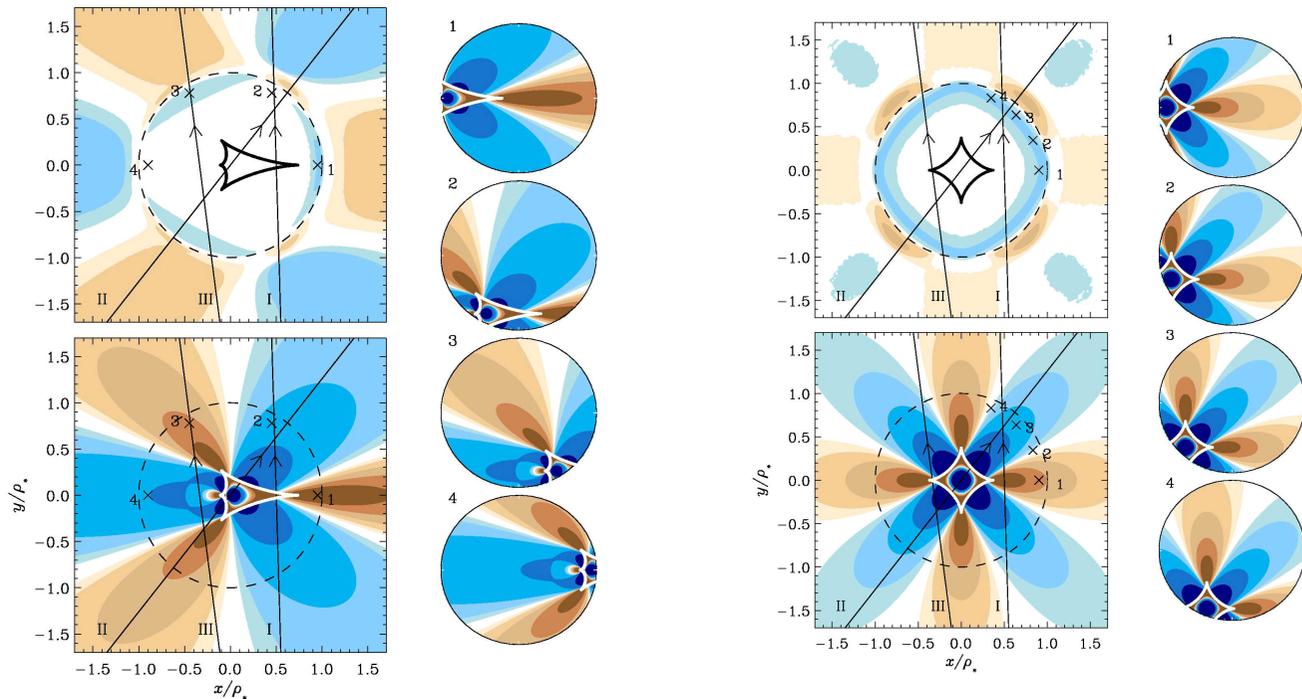


Fig 9. Morphology of central perturbation induced by a planet.

Fig 10. Morphology of central perturbation induced by a wide-separation binary companion.

- The most prominent difference shows up in the **morphology** of the **edge feature with negative excess**.
 - **Binary lensing**: The edge feature forms a complete circle.
 - **Planetary lensing**: The edge feature appears as several arc segments.

- The difference is basically caused by the difference in caustic shape.
 - **Binary lensing**: symmetric
 - **Planetary lensing**: asymmetric and elongated

□ **Diagnostic**

The absence of a well-developed dip in the residual from the single-lensing light curve at both or either of the moments of the caustic center's entrance into and exit from the source star surface indicates that the perturbation is produced by a planetary companion.

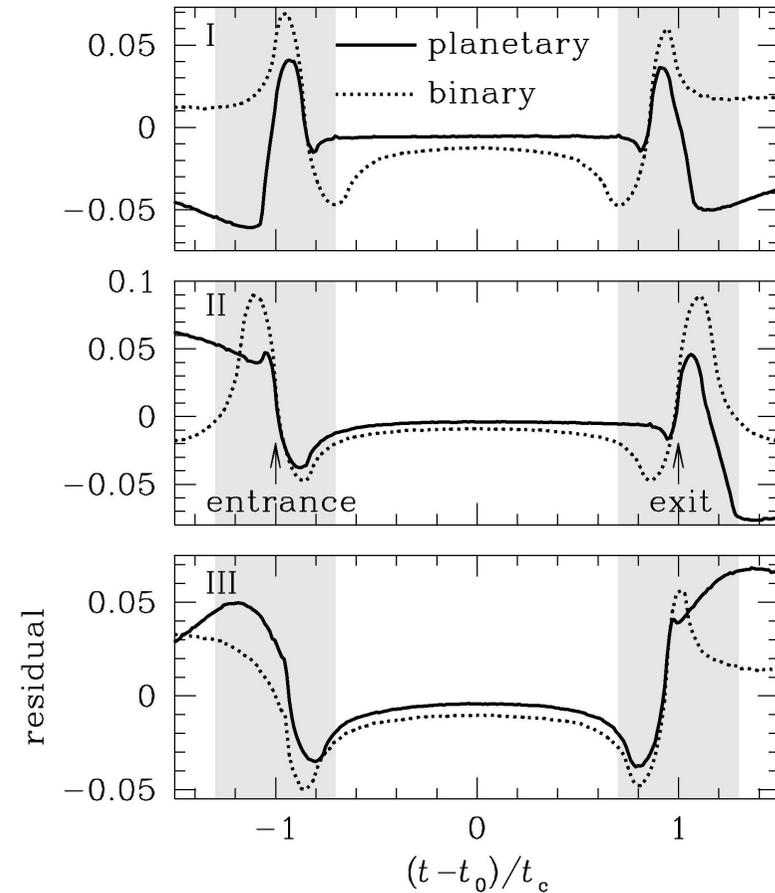


Fig 11. Residuals from single lensing for events produced by a planetary and a wide-separation binary systems.

Planet/Binary Degeneracy III

□ A diagnostic applicable to caustic-crossing events

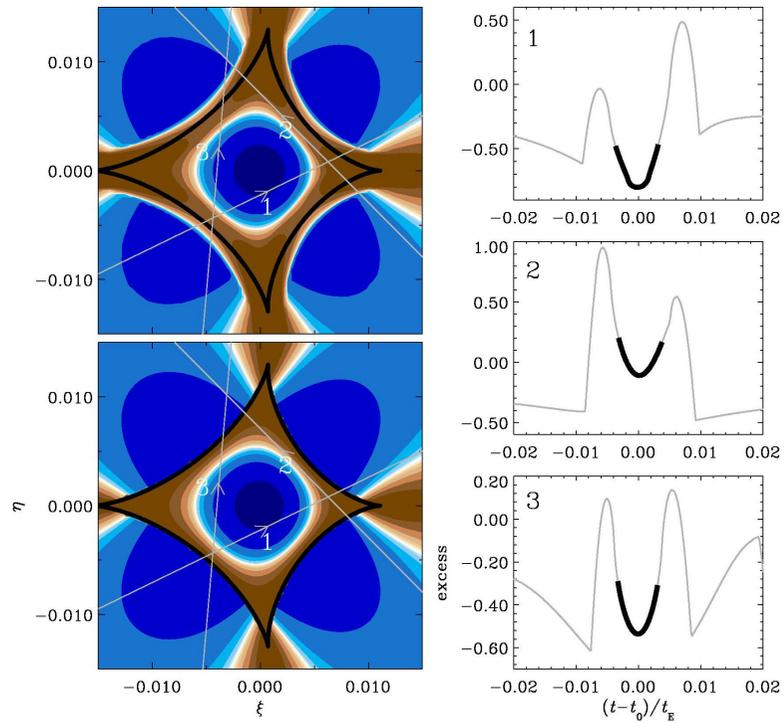


Fig 13. Morphology of central perturbation induced by a planet.

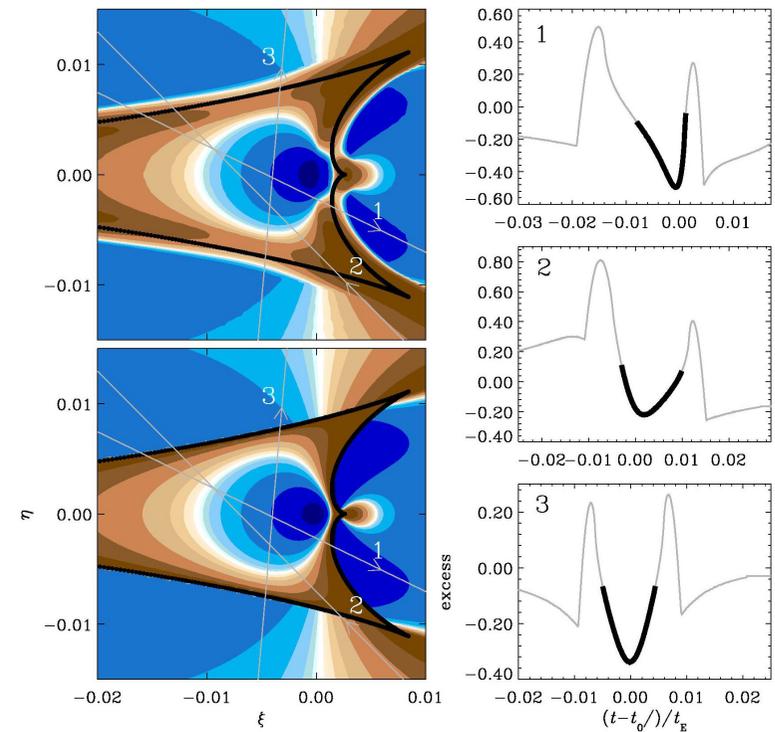


Fig 12. Morphology of central perturbation induced by a wide-separation binary.

- **Morphology of perturbation inside caustics**
 - **Binary lensing**: concentric circular pattern around the caustic center
 - **Planetary lensing**: elongated and off-centered

- **Diagnostic**
 - Distinctive features of the individual lens populations in the residual of the trough region between the two peaks of the caustic crossings.
 - **Binary lensing**: symmetric residual
 - **Planetary lensing**: asymmetric in general

- **Applicability**
 - The proposed diagnostic is useful for massive planets, which would be most common.

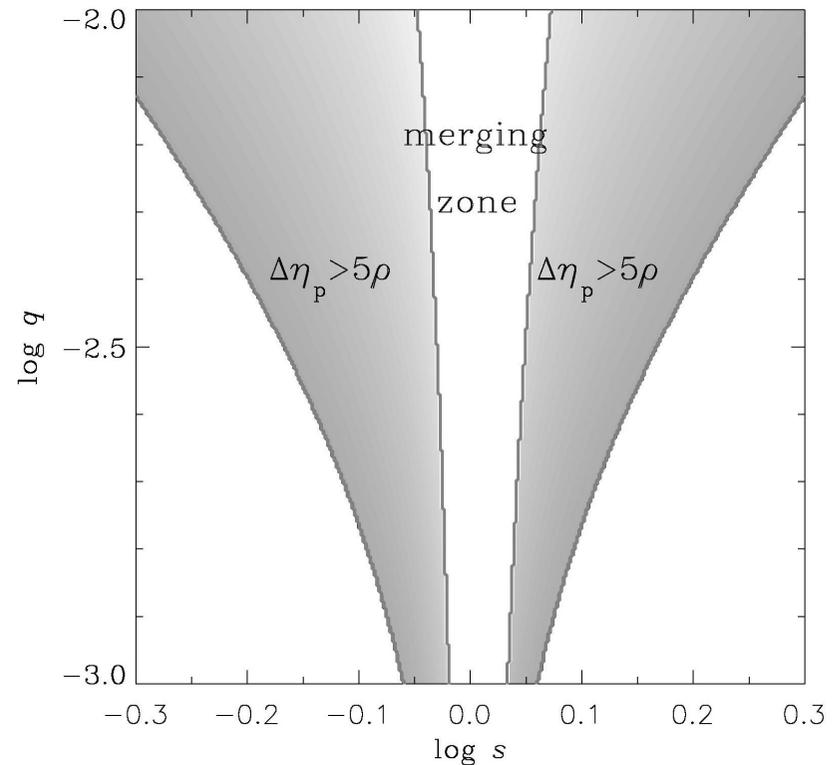


Fig 14. Ranges in the parameter space where the proposed diagnostics can be applicable.

Close/Wide Degeneracy ($s \leftrightarrow s^{-1}$ degeneracy)

- Perturbations induced by a planet with a projected separation in units of the Einstein radius, s , is very similar to the perturbation induced by a planet with a separation $1/s$.
- In what cases can this degeneracy resolved?

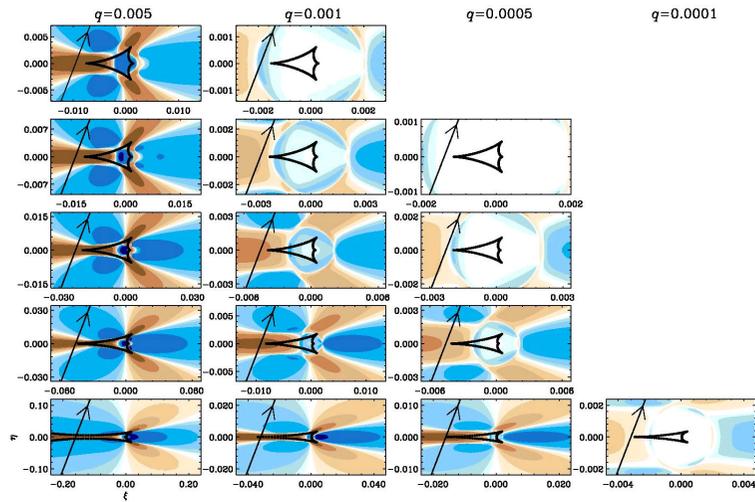


Fig 16. Color-scale maps of magnification excess for planets with separation from the star greater than the Einstein radius ($s > 1$). Brown is positive excess and blue is negative excess. Color-scale becomes darker at the excess levels of 1%, 2%, 4%, 8%, 16%, and 32%.

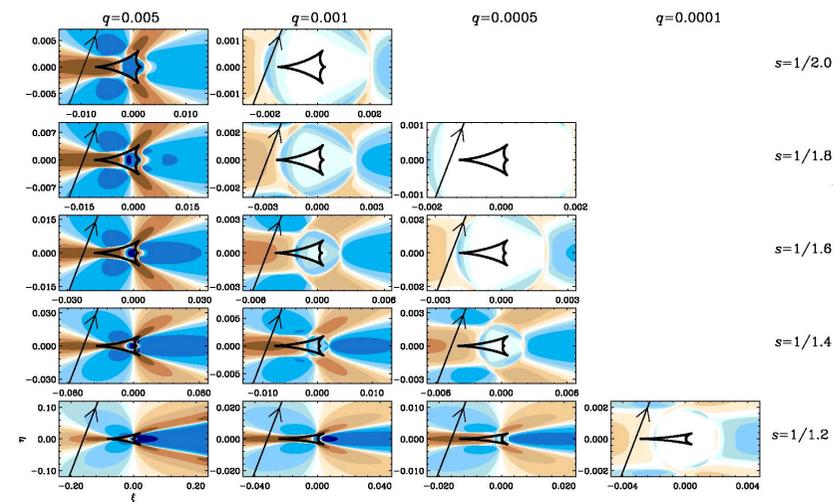


Fig 15. Color-scale maps of magnification excess for planets with separation from the star less than the Einstein radius ($s < 1$).

□ Tendencies

- Although similar, the patterns of perturbations induced by a close and wide planets are not identical.
- The magnification difference becomes larger as the [planet/primary mass ratio increases](#) and [primary-planet separation approaches the Einstein radius](#).
- For a given pair of a close and a wide planets, the region of major difference is confined in the region around the line connecting the central and the planetary caustics.

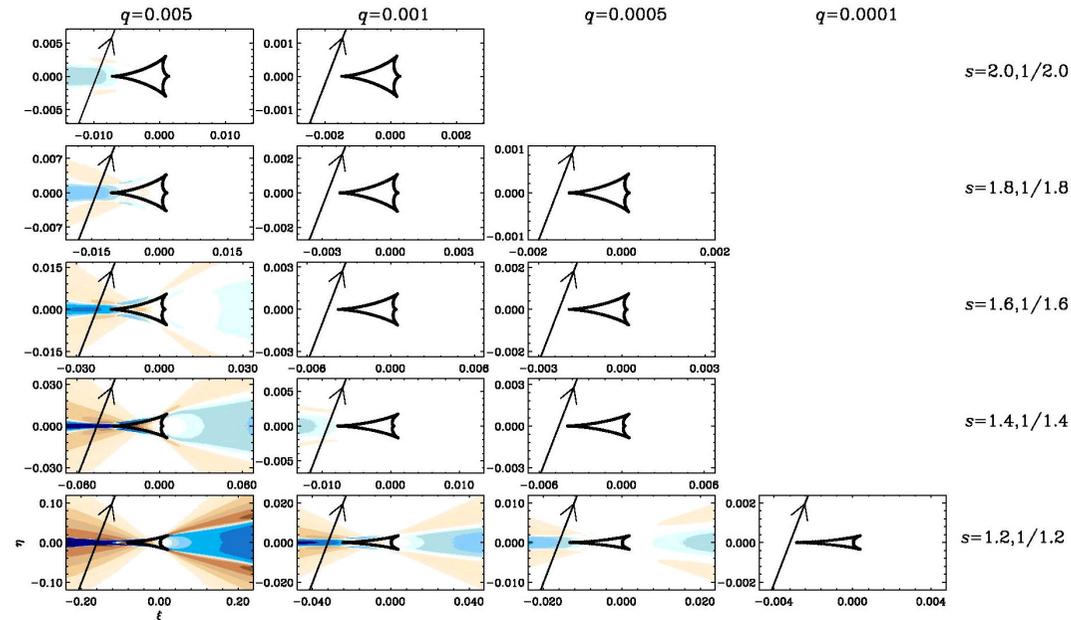


Fig 17. Color-scale maps of the difference in the magnification excess between close and wide planetary systems.

□ Cause of the difference

- The difference between the perturbation patterns of close and wide planets are due to the effect of the planetary caustic.
- Central perturbation is not isolated and instead it is connected to the region of perturbation induced by the planetary caustic.
- As the planet/primary mass ratio increases and the planet–primary separation approaches the Einstein radius, the planetary caustic becomes bigger and its effect on the central perturbation region increases. → This matches the tendency of the difference between the central perturbations induced by the close and a wide planets.

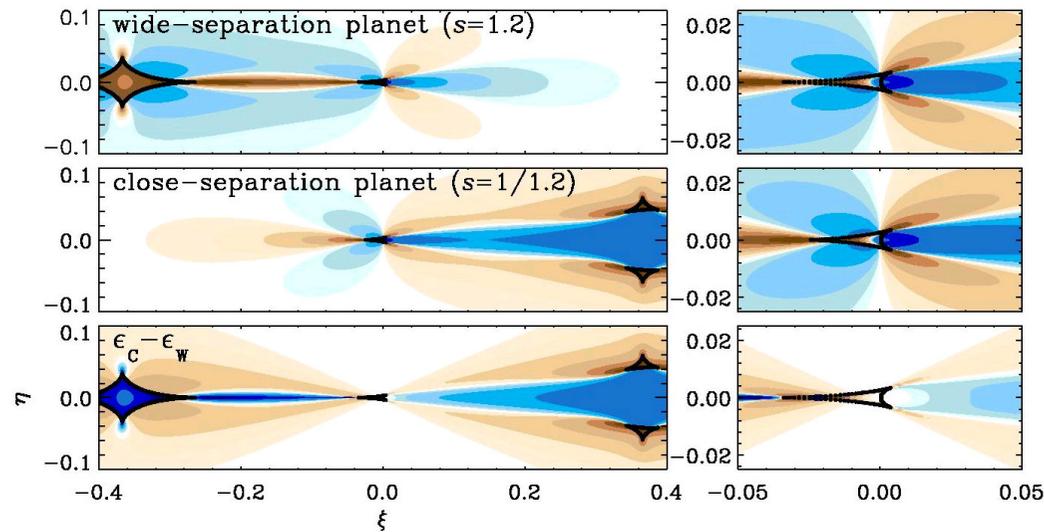


Fig 18. Maps of magnification excess (upper two panels) and excess difference (bottom panel) for an example pair of a close and a wide planet.